

## Mathematics Methods Units 3,4 Test 6 2019

# Calculator Assumed Sample Proportions & Confidence Intervals

STUDENT'S NAME	

**DATE**: Thursday 5<sup>th</sup> September **TIME**: 50 minutes **MARKS**: 43

#### **INSTRUCTIONS:**

Standard Items: Pens, pencils, drawing templates, eraser

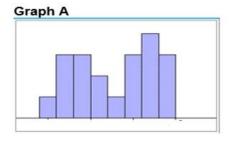
Special Items: Three calculators, notes on one side of a single A4 page (these notes to be handed in with this

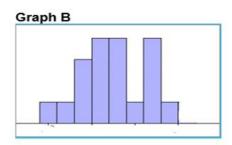
assessment)

Questions or parts of questions worth more than 2 marks require working to be shown to receive full marks.

#### 1. (2 marks)

A random sample is simulated from a uniform distribution. The following two graphs represent possible sampling distributions with one representing a sample of size 20 and the other a sample size of 100.

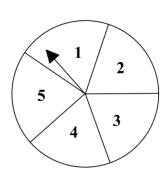




Which graph would best represent the sample of 100? Give a reason for your answer.

#### 2. (6 marks)

The spinner shown has each region equally likely to occur.



Suppose we wish to investigate the likelihood of achieving an even number on a spin. The spinner is spun 120 times resulting in 53 even numbers.

- (a) State the value of  $\hat{p}$  for this sample.
- (b) Calculate the value of  $\frac{\hat{p}-p}{\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}}$  using your value of  $\hat{p}$  from (a). [3]

(c) Sample proportions for multiple samples of 120 spins are recorded. The statistic in (b) is then calculated for each, describe the distribution of these values. [2]

[1]

(7 ma	xs)		
	mate the proportion of Western Australian high school students that play the pian of 200 students is taken.	10, a	
Of th	200 students in the sample, it was found that 178 students played the piano.		
(a)	Use this sample to estimate the:		
	(i) true proportion of Western Australian high school students that play the p	piano, [1]	
	(ii) standard deviation of sample proportions of Western Australian high schedulents that play the piano.	ool [2]	
(b)	If this sample was taken from a high school that specialises in music, discuss wi reasons the accuracy of the estimate of the true proportion of Western Australian school students that play the piano.		
The t	te proportion of Western Australian high school students that play the piano is 0.2	29.	
(c)	If the sample was taken from an ordinary high school, suggest two possible rand sampling techniques which could have been used.	om [2]	

3.

(8 ma	(8 marks)					
In a r	In a randomly selected sample of 50 residents from a city, 16 were born overseas.					
(a)	Use this sample to determine $\hat{p}$ , the sample proportion of overseas born residents in this city.					
	[1]					
(b)	Use this sample to provide a 90% confidence interval for $p$ . [3]					
(c)	In a second sample of 80 residents, 32 were overseas-born. Use your answer in (b) to determine with reasons if this sample statistically has a higher proportion of overseas					
	born residents. [2]					
(d)	Using the sample proportion of the survey from part (a), determine a smallest sample					
	size that will give at most a 10% margin of error with a confidence of 90%. [2]					

4.

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In a sample of n houses, 27 were found to have smoke detectors. Using this sample, a c % confidence interval for the true proportion of houses with smoke detectors was  $0.26 \le p \le 0.46$ .

(a) Calculate the value of n.

[2]

(b) Calculate the value of c.

[5]

#### 6. (4 marks)

It is known that p % of students in a certain state of Australia are international students. 50 samples of 100 students are taken and the proportions of international students were calculated. The sampling distribution of the sample proportions has a standard deviation of 0.035. Determine with reasons, a reasonable value of p.

(5 ma	(5 marks)					
A reco	ent survey indicated that 56% of Australians are in favour of Australia becomblic.	ing a				
(a)	Assuming that this proportion represents the population proportion, how mashould be surveyed to ensure that the 95% confidence interval for the surve of less than 2%?					
(b)	Assuming that the margin of error remains the same, what would be the effective of the sample if:	of error remains the same, what would be the effect on the				
	(i) the population proportion of those in favour was much higher?	[1]				
	(ii) the survey required a 99% level of confidence?	[1]				

7.

### 8. (4 marks)

When taking samples of size 400 from a population, it was found that 6% of samples had a proportion that was more than 0.03 above the population proportion. Determine the population proportion.